

Contribution

We use cooperative manipulators to perform towel folding tasks. Our method executes a *momentum fold*: a swinging motion that exploits the object's dynamics. We propose a new learning algorithm that combines imitation and reinforcement learning.

The strengths of the algorithm come from its efficient processing, fast learning capabilities, absence of a deformable object model, and applicability to other problems exhibiting temporally incoherent parameter spaces.

Reward Function

Computing $R(O^c)$:

```

minAvgError ← 1000
for all  $O_i \in O^t$  do
  Training ← LastFrame( $O_i$ )
  Current ← LastFrame( $O^c$ )
  AvgError ← ICP(Training, Current)
  if AvgError ≤ minAvgError then
    minAvgError ← AvgError
  end if
end for
return  $\exp(-minAvgError/100)$ 

```

Imitation Layer: Exploratory

- Explore trained action space with robot
- Looking for most diverse set of examples
- Lloyd's k-means clustering algorithm

$$\arg \min_C \sum_{j=1}^M \sum_{\theta_i \in C_j} \|\theta_i - \mu_j\|$$

$$\theta^{Epl} = [\theta_1^{Epl} \dots \theta_M^{Epl}] \text{ s.t. } \theta_i^{Epl} \in C_i \in \theta^t$$

Imitation Layer: Expansion

- Expand best robot action based on θ_{Best}^{Epl}
- Run PCA on O^t to get $\hat{O}^t \in \mathbb{R}^{80 \times 29}$
- Train Radial Basis Functions (RBF) on \hat{O}^t
- Generate l new actions, θ_s^{Epa} , using:

```

n = NumColumns( $\hat{O}^t$ ) // n=29
 $\hat{O}^t \sim [\hat{O}_1^t \hat{O}_2^t \dots \hat{O}_n^t]$ 
 $\mu = [E[\hat{O}_1^t] \ E[\hat{O}_2^t] \ \dots \ E[\hat{O}_n^t]]$ 
 $\Sigma = [Cov(\hat{O}_i^t, \hat{O}_j^t)]_{i=1,2,\dots,n; j=1,2,\dots,n}$ 
repeat

```

Sample \hat{O}^s from $\mathcal{N}(\mu, \Sigma)$

until $|\text{Time}(\hat{O}^s) - \text{Time}(\theta_{Best}^{Epl})| \leq \epsilon$

$\theta_s^{Epa} = \text{RBF}(\hat{O}^s)$

return θ_s^{Epa}

$$\theta^{Epa} = [\theta_1^{Epa} \theta_2^{Epa} \dots \theta_l^{Epa}]$$

Reinforcement Learning Layer

- θ_n^{RL} is updated to produce a new action θ_{n+1}^{RL}
- $\theta_{n+1}^{RL} = \theta_n^{RL} + (\theta_{Top} - \theta_n^{RL}) [R(O_{Top}) - R(O_n)]$
- θ_{Top} corresponds to the best rewards of:

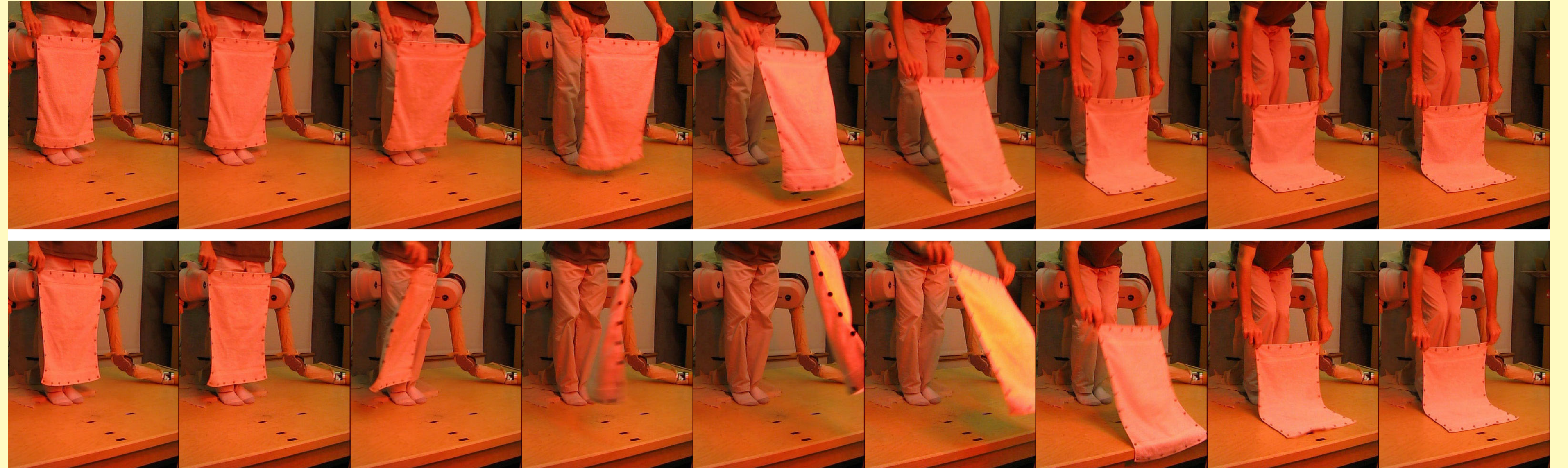
$$[\theta_{Best}^{Epl} \theta_1^{Epa} \dots \theta_l^{Epa} \theta_1^{RL} \dots \theta_{n-1}^{RL}]$$

Acknowledgement

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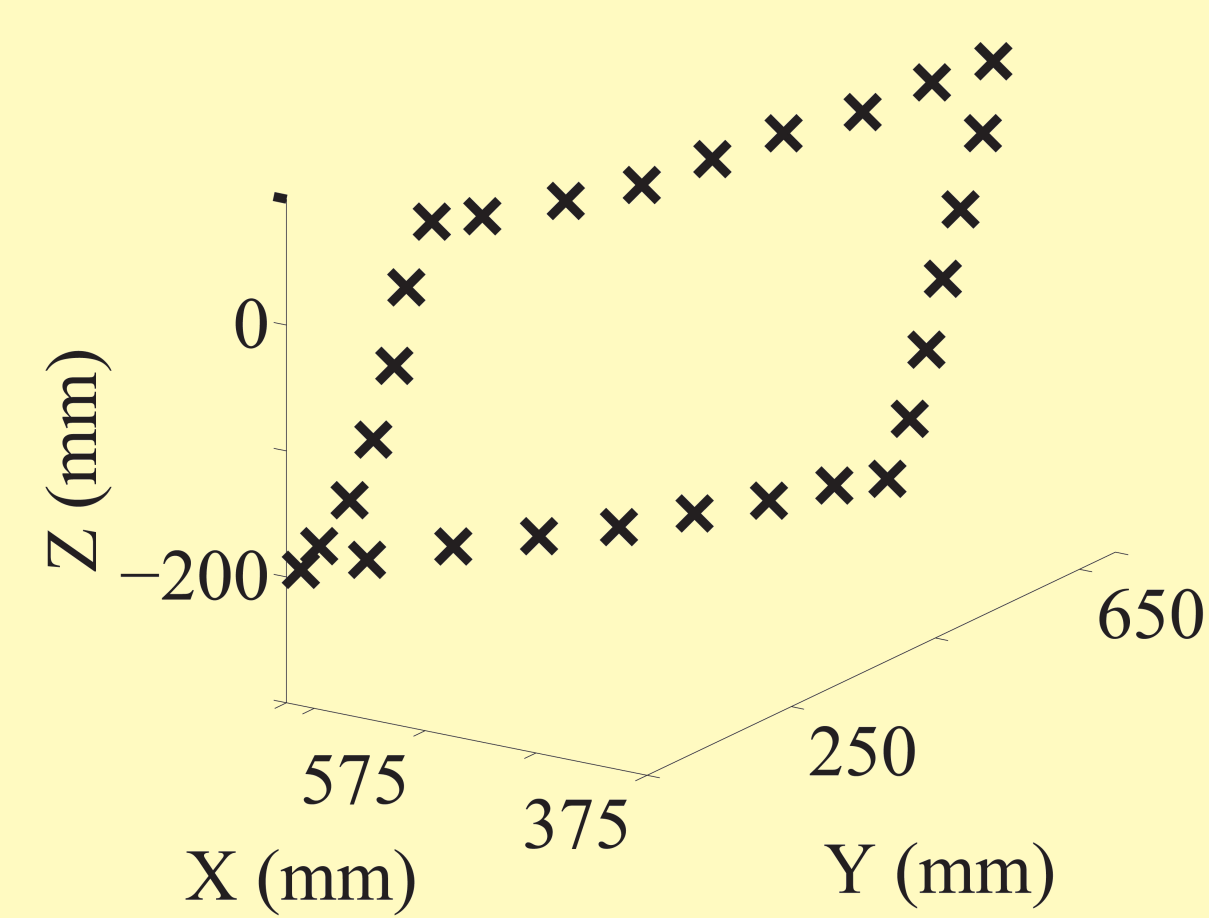
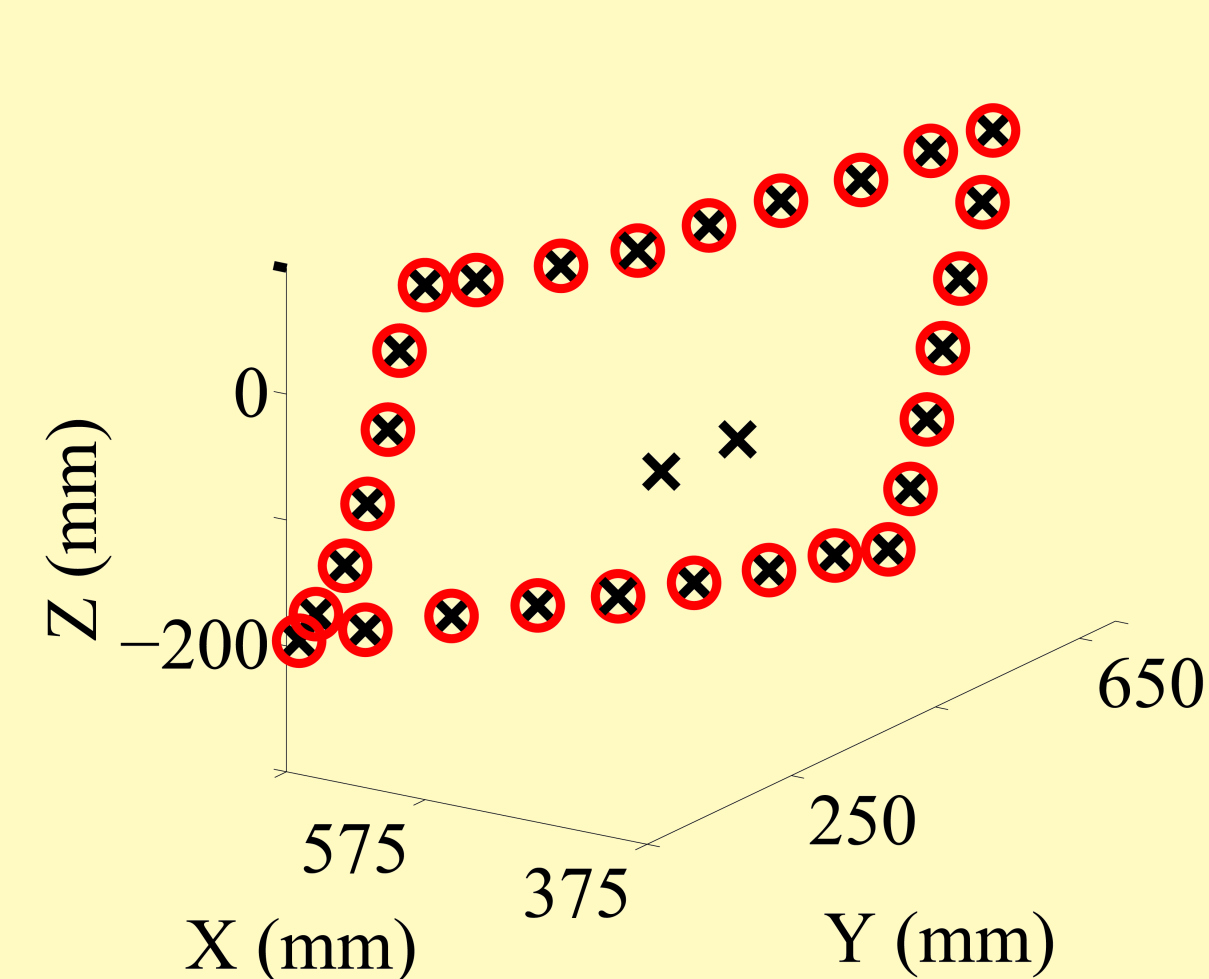
Imitation Learning

- **Motion capture system:** Cartesian coordinates and time stamp of 28 markers recorded at 30 Hz
- **Action/Observation pairs:** $\theta_i \in \mathbb{R}^{1050}$ and $O_i \in \mathbb{R}^{12750}$
- **Complete training data set:** $\theta^t \in \mathbb{R}^{80 \times 1050}$ and $O^t \in \mathbb{R}^{80 \times 12750}$



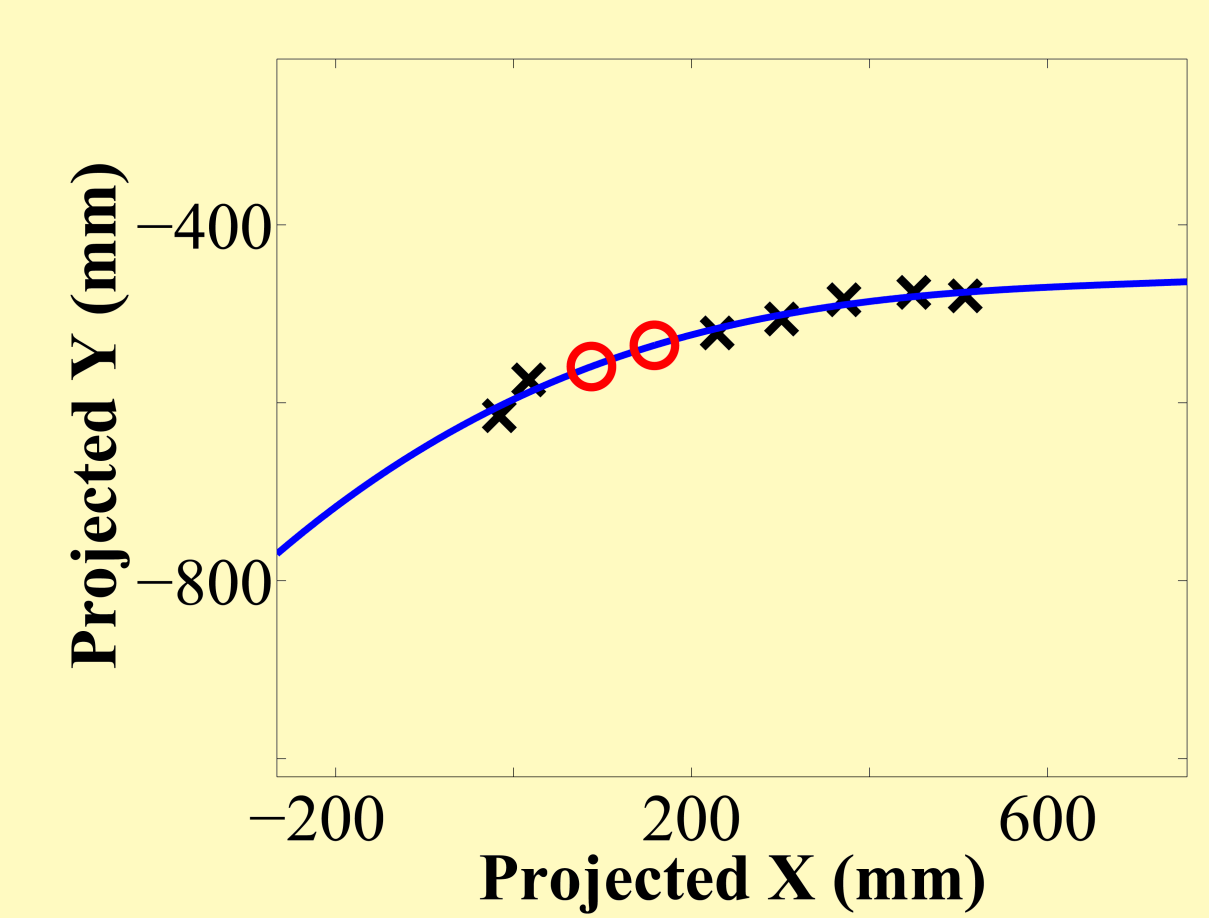
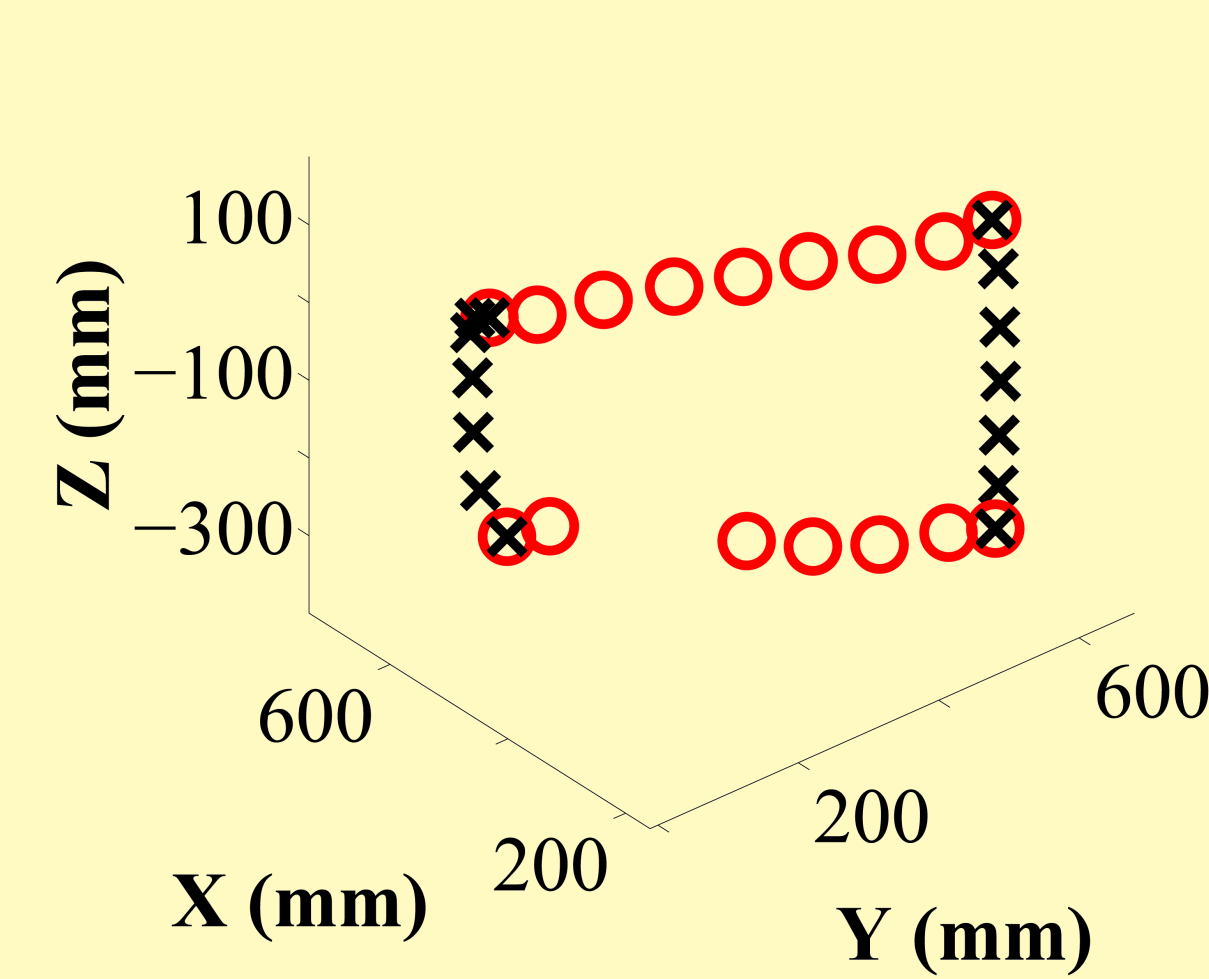
Correcting False Positives and False Negatives

False Positives



100% Correction Rate

False Negatives



88.89% Correction Rate

Results and Experiments

- Robot configurations acquired through 7-DoF IK
- Joint minimization to reduce mechanical loads
- **Training Data:** 80 examples
- **Exploratory Layer:** 10 runs
- **Expansion Layer:** 5 runs
- **Reinforcement Learning:** until convergence
 - Difference in last 3 rewards $\leq 0.1\%$
 - Converges in only 4 trials
 - Good seed due to exploratory and expansion layers

